

[All Pythagorean triples]

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All Pythagorean triples cannot be the power numbers.
 The figure (XY) cannot be the power number in co prime (A,B).

$$X=(2AB)^{1/2}+A, Y=(2AB)^{1/2}+B, Z=(2AB)^{1/2}+A+B$$

$$2AB=k^2(k \text{ is } 1,2,3\dots)$$

$$XY=k(k+A)(k+2A)/2A=k(k+B)(k+2B)/2B$$

$$\text{When } A=c^2, B=2d^2$$

$$XY=2cd(c+d)(c+2d)$$

The figure $2cd(c+d)(c+2d)$ cannot be the power number in co prime (c,d).

$$\text{When } c=e^n, d=2^{(n-1)}f^n$$

$$(2ef)^n\{e^n+2^{(n-1)}f^n\}[e^n+2\{2^{(n-1)}f^n\}]=2(efst)^n$$

The numbers (s,t) cannot be the natural numbers.

$$\{e^n+2^{(n-1)}f^n\}[e^n+2\{2^{(n-1)}f^n\}]=(st)^n$$

$$\{e^n+2^{(n-1)}f^n\}=s^n$$

$$\{s^n+2^{(n-1)}f^n\}=t^n$$

$$1=(t^n-s^n)/(s^n-e^n), 2s^n=t^n+e^n$$

$$\{e^n+f+1\}\{e^n+2(f+1)\}=(st)^n$$

$$\{e^n+f+1\}=s^n$$

$$\{s^n+f+1\}=t^n$$

$$1=(t^n-s^n)/(s^n-e^n), 2s^n=t^n+e^n$$

$$\{e^n+f\}\{e^n+2(f)\}=(st)^n$$

$$\{e^n+f\}=s^n$$

$$\{s^n+f\}=t^n$$

$$1=(t^n-s^n)/(s^n-e^n), 2s^n=t^n+e^n$$

⋮

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⋮

$$\{e^n+2\}\{e^n+2(2)\}=(st)^n$$

$$\{e^n+2\}=s^n$$

$$\{s^n+2\}=t^n$$

$$1=(t^n-s^n)/(s^n-e^n), 2s^n=t^n+e^n$$

$$\{e^n+1\}\{e^n+2\}=(st)^n$$

$$\{e^n+1\}=s^n$$

$$\{s^n+1\}=t^n$$

$$1=(t^n-s^n)/(s^n-e^n), 2s^n=t^n+e^n$$

Therefore, the numbers (s,t) cannot be the natural numbers.